

# ECONOMETRIC METHODS II: TIME SERIES

## HOME WORK 1

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### INSTRUCTIONS

Write up your results and submit electronically (preferably in pdf format) to knimark@crei.cat before 17.00 Thursday June 11 together with any MatLab code used in the exercise. You may work in groups of up to three people. Please list all names of persons in the group on the front page. To answer the questions, you will need to download the data file `HW1data.mat` from the course web page at [http://www.kris-nimark.net/TS\\_UPF\\_2009.html](http://www.kris-nimark.net/TS_UPF_2009.html) .

### QUESTION 1: FINDING THE STRUCTURAL COEFFICIENT MATRICES 4PTS

The data file `HW1data.mat` contains 101 quarters of fictional GDP growth rates ( $\Delta GDP_t$ ) and unemployment ( $U_t$ ) collected in a  $(2 \times 101)$  matrix of the form

$$\text{HW1data.mat} = \begin{bmatrix} \Delta GDP_0 & \Delta GDP_1 & \cdots & \Delta GDP_T \\ U_0 & U_1 & \cdots & U_T \end{bmatrix}$$

Both  $\Delta GDP_t$  and  $U_t$  are demeaned and stationary. Find the structural form coefficient matrices  $A_0$  and  $A_1$  in

$$A_0 y_t = A_1 y_{t-1} + \mathbf{u}_t$$

where

$$\begin{aligned} y_t &= \begin{bmatrix} \Delta GDP_t \\ U_t \end{bmatrix} \\ \mathbf{u}_t &= \begin{bmatrix} u_t^s \\ u_t^d \end{bmatrix} \\ E[u_t u_t'] &= I \end{aligned}$$

by using Blanchard and Quah's (1989) identification scheme, i.e. that demand shocks  $u_t^d$  have no permanent effect on GDP *levels*. (Remember:  $\Delta GDP_t \equiv GDP_t - GDP_{t-1}$ )

**Hint:** The Cholesky decomposition decomposes *any* symmetric positive definite matrix  $S$  into the form  $TT' \equiv S$  where  $T$  is lower triangular. If  $\Sigma$  is a covariance matrix, then for any  $B$ , the matrix  $B\Sigma B'$  is symmetric and positive semi definite.

## QUESTION 2: IMPULSE RESPONSE FUNCTIONS 2PTS

a) Derive and plot the impulse response functions describing the effects of a unit shock to  $u_t^s$  and  $u_t^d$  on  $y_t$ . I.e. find

$$\frac{\partial \Delta GDP_{t+j}}{\partial u_t^i} : i = s, d \text{ and } j = 0, 1, 2, \dots, 50.$$

$$\frac{\partial U_{t+j}}{\partial u_t^i} : i = s, d \text{ and } j = 0, 1, 2, \dots, 50.$$

How does the plot(s) relate to the identifying assumption?

b) Derive and plot the impulse response functions describing the effects of a unit shock to  $u_t^s$  and  $u_t^d$  on the level of GDP, i.e. find

$$\frac{\partial GDP_{t+j}}{\partial u_t^i} : i = s, d \text{ and } j = 0, 1, 2, \dots, 50.$$

How does the plot relate to the identifying assumption?

## QUESTION 3: VARIANCE DECOMPOSITIONS 2PTS

Compute the fractions of the variances of  $\Delta GDP_t$  and  $U_t$  attributable to  $u_t^s$  and  $u_t^d$ , respectively.

## QUESTION 4: HISTORICAL DECOMPOSITIONS 2PTS

Decompose the history of  $\Delta GDP_t$  and  $U_t$  into the contributions of past  $u_t^s$ ,  $u_t^d$  and initial conditions  $y_0$ . That is, decompose  $y_t$  for each  $t = 1, 2, \dots, T$  into the three terms  $a_t y_0$ ,  $\sum_{j=0}^{t-1} b_j u_{t-j}^s$  and  $\sum_{j=0}^{t-1} c_j u_{t-j}^d$  for  $j = 1, 2, \dots, (t-1)$ . (I.e. find the  $a, b$  and  $c$ s.) Plot the results. What is the value of  $y_t - a_t y_0 - \sum_{j=0}^{t-1} b_j u_{t-j}^s - \sum_{j=0}^{t-1} c_j u_{t-j}^d$ ?